

Name: _____

Read all directions and problems carefully! Show all appropriate work for credit.

1. For the function, $g(x) = -x^3 - 3x^2 + 9x + 15$;
 - ✓ a) Determine the critical numbers and then write the critical points of the function, $g(x)$.
 - ✓ b) Write the intervals, using interval notation, on which $g(x)$ is increasing and decreasing.
 - ✓ c) Use the First Derivative test to locate the local maximum and minimum values. Describe explicitly how this test was used to determine a max or a min.
 - ✓ d) Determine the inflection numbers and then write the inflection points of the function, $g(x)$.
 - e) Write the intervals, using interval notation, on which $g(x)$ is concave up and concave down.

$$g(x) = -x^3 - 3x^2 + 9x + 15$$

$$g'(x) = -3x^2 - 6x + 9$$

$$= -3(x^2 + 2x - 3) = 0 \quad \leftarrow \text{Finding CN's}$$

$$= -3(x+3)(x-1)$$

$$x = -3 \text{ or } x = 1$$

$$g''(x) = -6x - 6$$

$$= -6(x+1) = 0$$

$$x = -1$$

a) CN: $x = -3 + 1$ ✓

$$g(-3) = -(-3)^3 - 3(-3)^2 + 9(-3) + 15$$

$$= +27 - 27 - 27 + 15$$

$$= -12$$

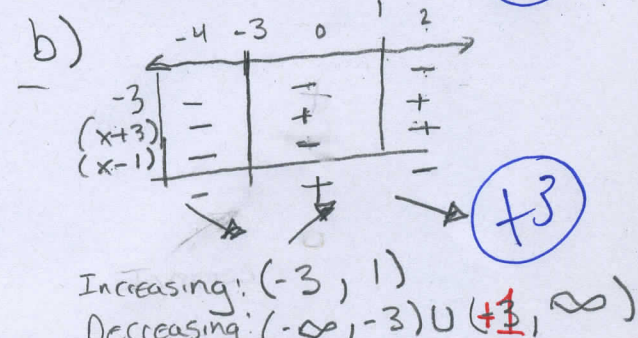
→ CP: $(-3, -12)$

$$g(1) = -(1)^3 - 3(1)^2 + 9(1) + 15$$

$$= -1 - 3 + 9 + 15$$

$$= 20$$

→ CP: $(1, 20)$ ✓ (+4)



c) Relative min of $y = -12$ @ $x = -3$
 Relative max of $y = 20$ @ $x = 1$

When the sign of the derivative switches it indicates you have a min or max. From "-" to "+" is a min and from "+" to "-" is a max. (+4)

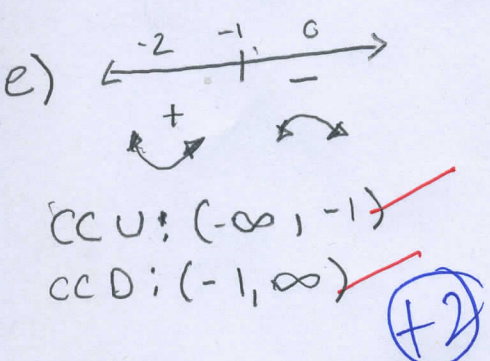
d) IN: $x = -1$

$$g(-1) = -(-1)^3 - 3(-1)^2 + 9(-1) + 15$$

$$= 1 - 3 - 9 + 15$$

$$= 4$$

IP: $(-1, 4)$ ✓ (+2)



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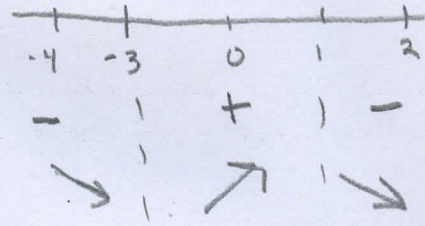
down. $g(x) = -x^3 - 3x^2 + 9x + 15$ $+27 - 27 - 27 + 15 = -12$
 $g'(x) = -3x^2 - 6x + 9$ $-1 - 3 + 9 + 15 = 20$

$g'(x) = -3(x^2 + 2x - 3) = -3(x-1)(x+3)$

a) $(x+3)(x-1) = x = -3, x = 1$
 CP = $(-3, -12)$ & $(1, 20)$ (+4)

a) C# = $x = -3, x = 1$
 CP = $(-3, -12)$ & $(1, 20)$

b) inc $(-3, 1)$
 Dec $(-\infty, -3) \cup (1, \infty)$



b) inc $(-3, 1)$
 Dec $(-\infty, -3) \cup (1, \infty)$ (+8)

c) Relative min at $(-3, -12)$ where sign of test goes from $-$ to $+$
 Relative max at $(1, 20)$ where sign of test goes from $+$ to $-$
 Relative because end behavior is \swarrow & \searrow Changing to positive so \rightarrow to \uparrow and \rightarrow to \downarrow means charge from increasing to decreasing

d) $g'(x) = -3x^2 - 6x + 9$
 $g''(x) = -6x - 6$
 IP = $y = 4$ at $x = -1$
 $IP = -6(x+1)$ $x = -1$ $g(-1) = 4$
 $g''(-1) = -6(-1) - 6 = 0$ (+2)

e) $g(x)$ is:
 concave up at $(-\infty, -1)$
 concave down at $(-1, \infty)$ (+2)

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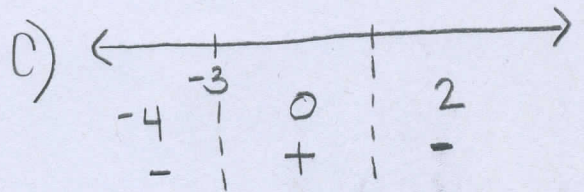
$$g(x) = -x^3 - 3x^2 + 9x + 15$$

$$g'(x) = -3x^2 - 6x + 9$$

$$= -3(x^2 + 2x - 3)$$

$$= -3(x-1)(x+3)$$

$x = 1 + x = -3$



$$0 = -3(-1)(3) = 9 +$$

$$2 = -3(1)(5) = -15$$

A) Critical numbers: $x = -3 + x = 1$

Critical points: $(1, 20), (-3, -12)$

$$g(1) = -(1)^3 - 3(1^2) + 9(1) + 15$$

$$= -1 - 3 + 9 + 15$$

$$g(1) = 20$$

$$g(-3) = -(-3)^3 - 3(-3^2) + 9(-3) + 15$$

$$= 27 - 27 - 27 + 15$$

$$g(-3) = -12$$

B) $(-\infty, -3) \cup (1, \infty)$: Decreasing
 $(-3, 1)$: Increasing

Decreasing: $(-\infty, -3), (1, \infty)$
 Increasing: $(-3, 1)$

REL. Maximum: $(1, 20)$ @ $x = 1$.
 REL. Minimum: $(-3, -12)$ @ $x = -3$.

This test would be used to determine a max or a min by when $g'(x)$ goes from decreasing to increasing you have a min & from increasing to decreasing you have a max.

$$g'(x) = -3x^2 - 6x + 9$$

$$g''(x) = -6x - 6$$

$$= -6(x+1) = 0$$

$$= x = -1$$

Inflection Numbers: $x = -1$

$$-(-1)^3 - 3(-1^2) + 9(-1) + 15$$

$$= 1 - 3 - 9 + 15 = 4$$

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